

What is balancing of rotating members?

Balancing means a process of restoring a rotor which has unbalance to a balanced state by adjusting the mass distribution of the rotor about its axis of rotation

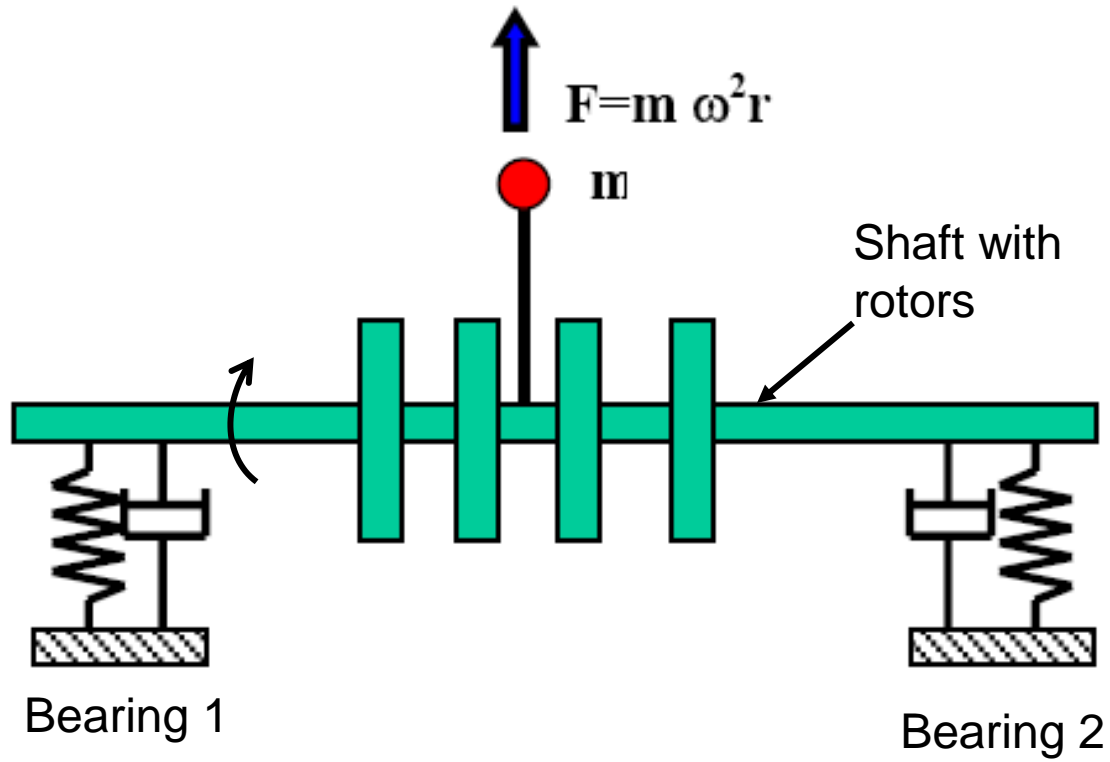
Balancing

"is the process of attempting to improve the mass distribution of a body so that it rotates in its bearings without unbalanced centrifugal forces"

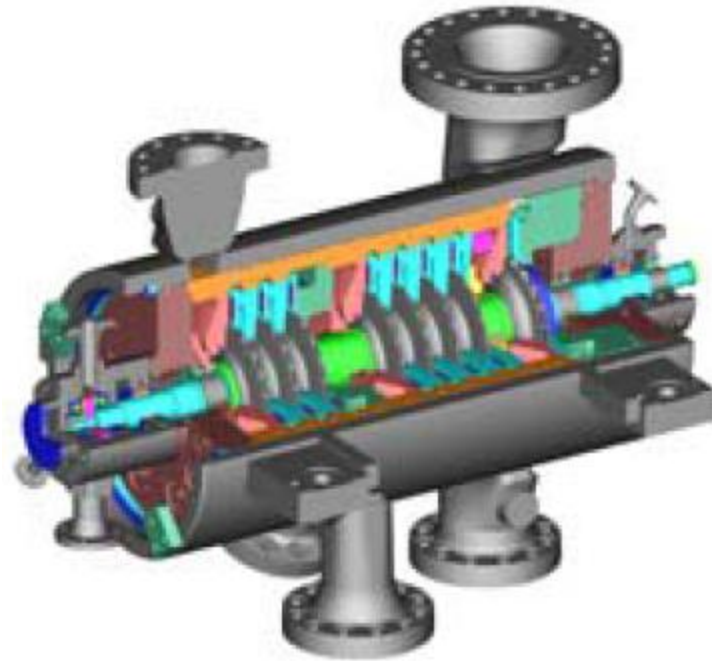
- Mass balancing is routine for rotating machines, some reciprocating machines, and vehicles
- Mass balancing is necessary for quiet operation, high speeds , long bearing life, operator comfort, controls free of malfunctioning, or a "quality" feel

Rotating components for balancing

- Pulley & gear shaft assemblies
- Starter armatures
- Airspace components
- High speed machine tool spindles
- flywheels
- Impellers
- Centrifuge rotors
- Electric motor rotors
- Fan and blowers
- Compressor rotors
- Turbochargers
- Precision shafts
- crank shafts
- Grinding wheels
- Steam & GasTurbine rotors



Unbalanced force on the bearing –rotor system

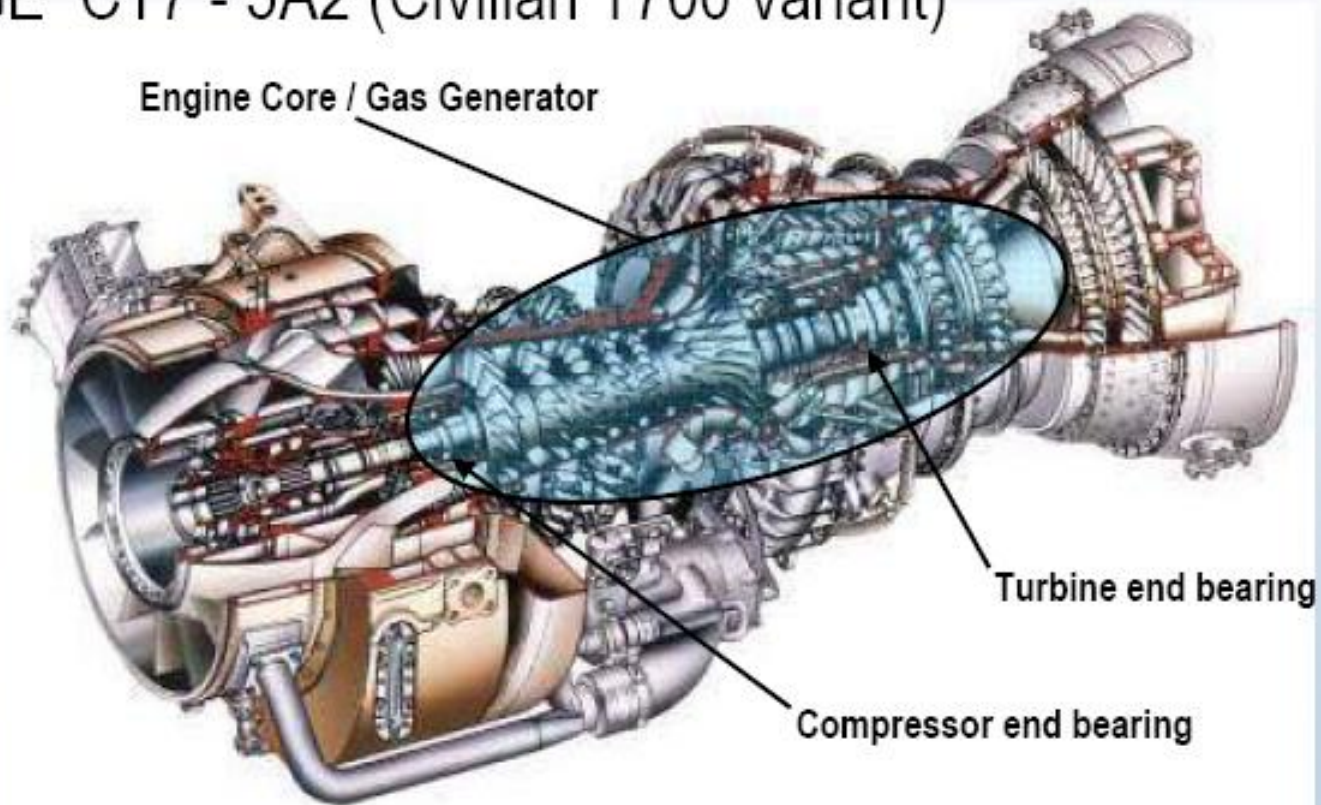


Cut away section of centrifugal compressor



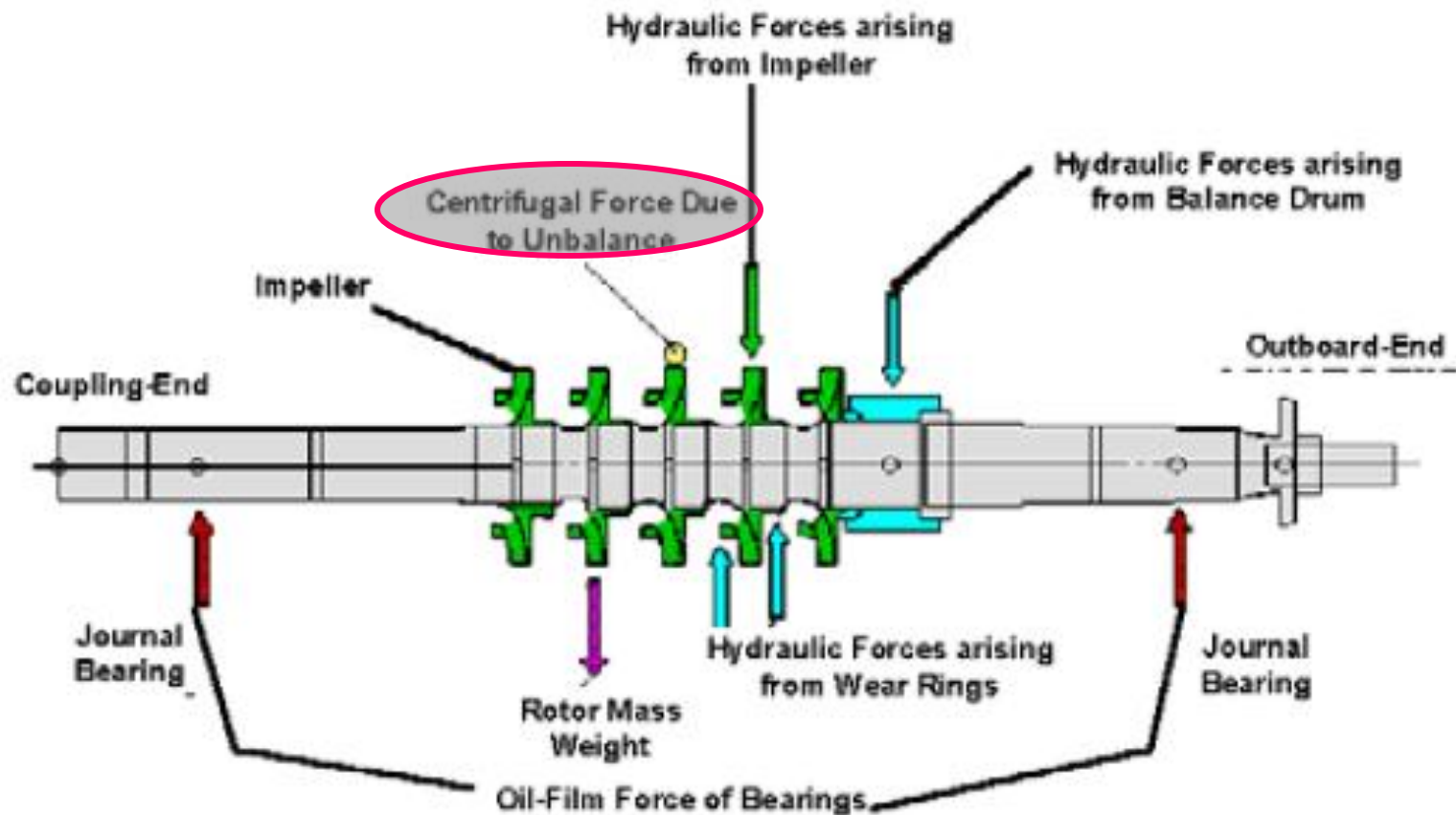
Common Rotary Wing Turboshaft Engine

- GE CT7 - 5A2 (Civilian T700 variant)





Radial forces Acting on Pump Rotor



- Unbalance is caused by the **displacement** of the **mass centerline from the axis of rotation**.
- **Centrifugal force** of "heavy" point of a rotor exceeds the centrifugal force exerted by the light side of the rotor and **pulls the entire rotor** in the direction of the heavy point.
- **Balancing** is the correction of this phenomena by the **removal or addition of mass**

Benefits of balancing

- Increase **quality** of operation.
- Minimize **vibration**.
- Minimize audible and signal **noises**.
- Minimize **structural fatigue stresses**.
- Minimize operator annoyance and **fatigue**.
- Increase **bearing life**.
- Minimize **power loss**.

NEED FOR BALANCING

Rotating a rotor which has unbalance causes the following problems.

- **The whole machine vibrates.**
- **Noise occurs due to vibration of the whole machine.**
- **Abrasion of bearings may shorten the life of the machine.**

Rotating **Unbalance occurs due to the following reasons.**

- The **shape of the rotor is unsymmetrical.**
- Un symmetrical exists due to a **machining error.**
- The **material is not uniform**, especially in Castings.
- A **deformation** exists due to a **distortion.**

- An **eccentricity** exists due to a gap of fitting.
- An **eccentricity** exists in the inner ring of rolling bearing.
- **Non-uniformity** exists in either **keys or key seats**.
- Non-uniformity exists in the **mass of flange**

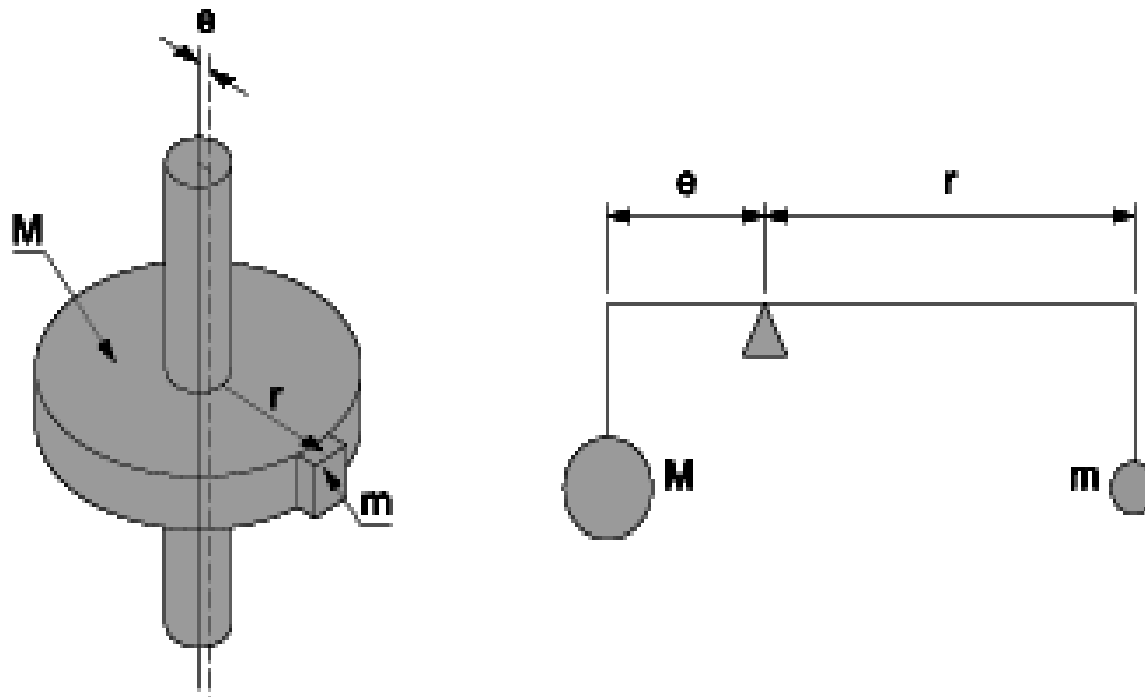
- Unbalance due to
**unequal distribution
of masses**
- Unbalance due to
unequal distance of masses

Types of Unbalance

Static Unbalance

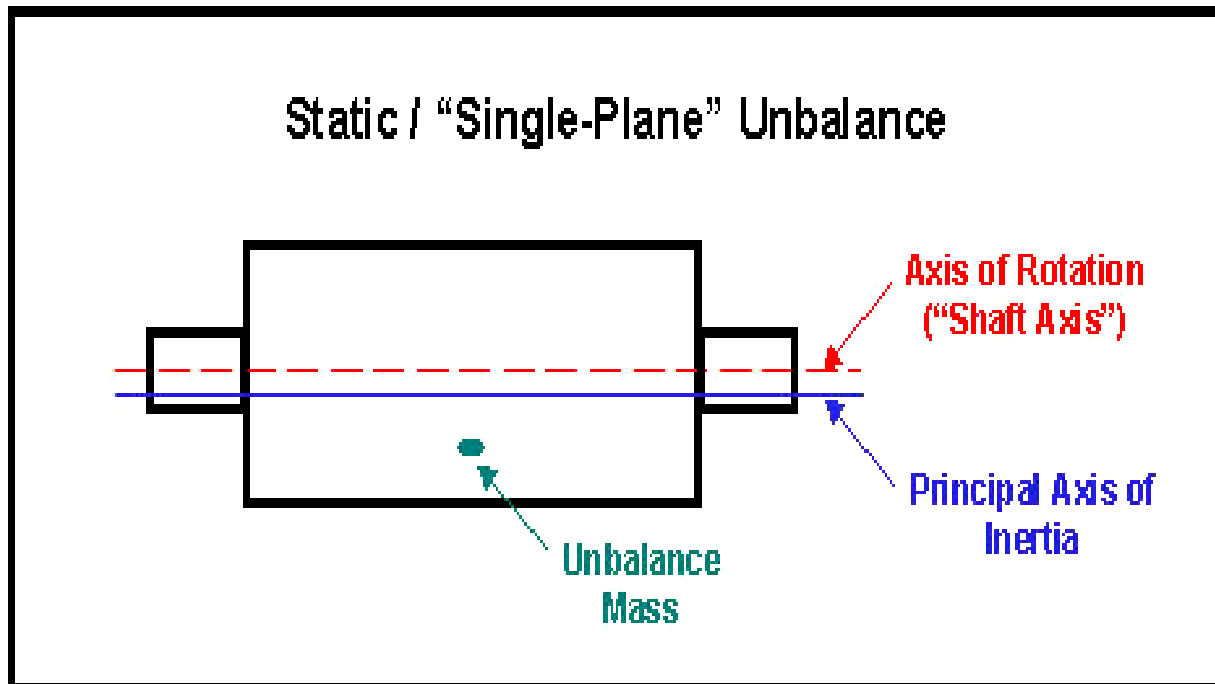
Dynamic Unbalance

STATIC BALANCING (SINGLE PLANE BALANCING)



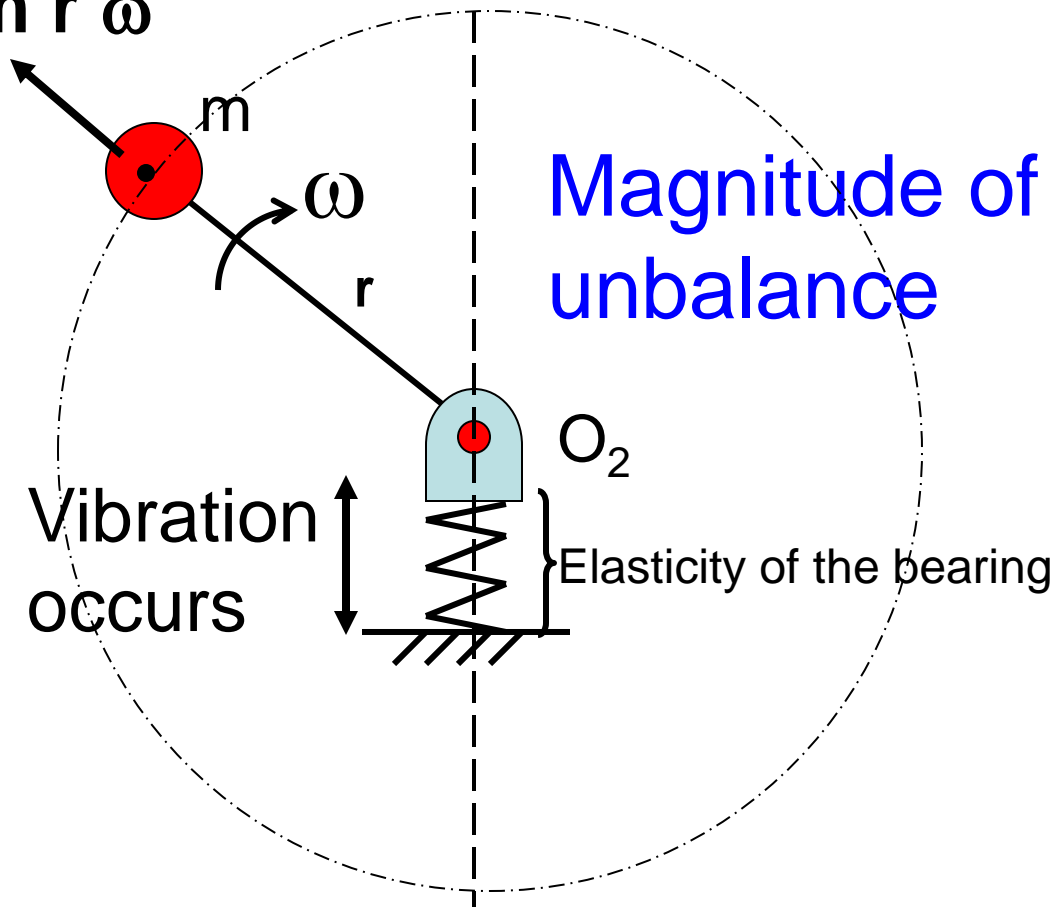
Single plane balancing. This is applied to thin disk-shaped rotors.

Single plane balancing



Adequate for rotors which are **short in length**, such as **pulleys and fans**

$$F = m r \omega^2$$



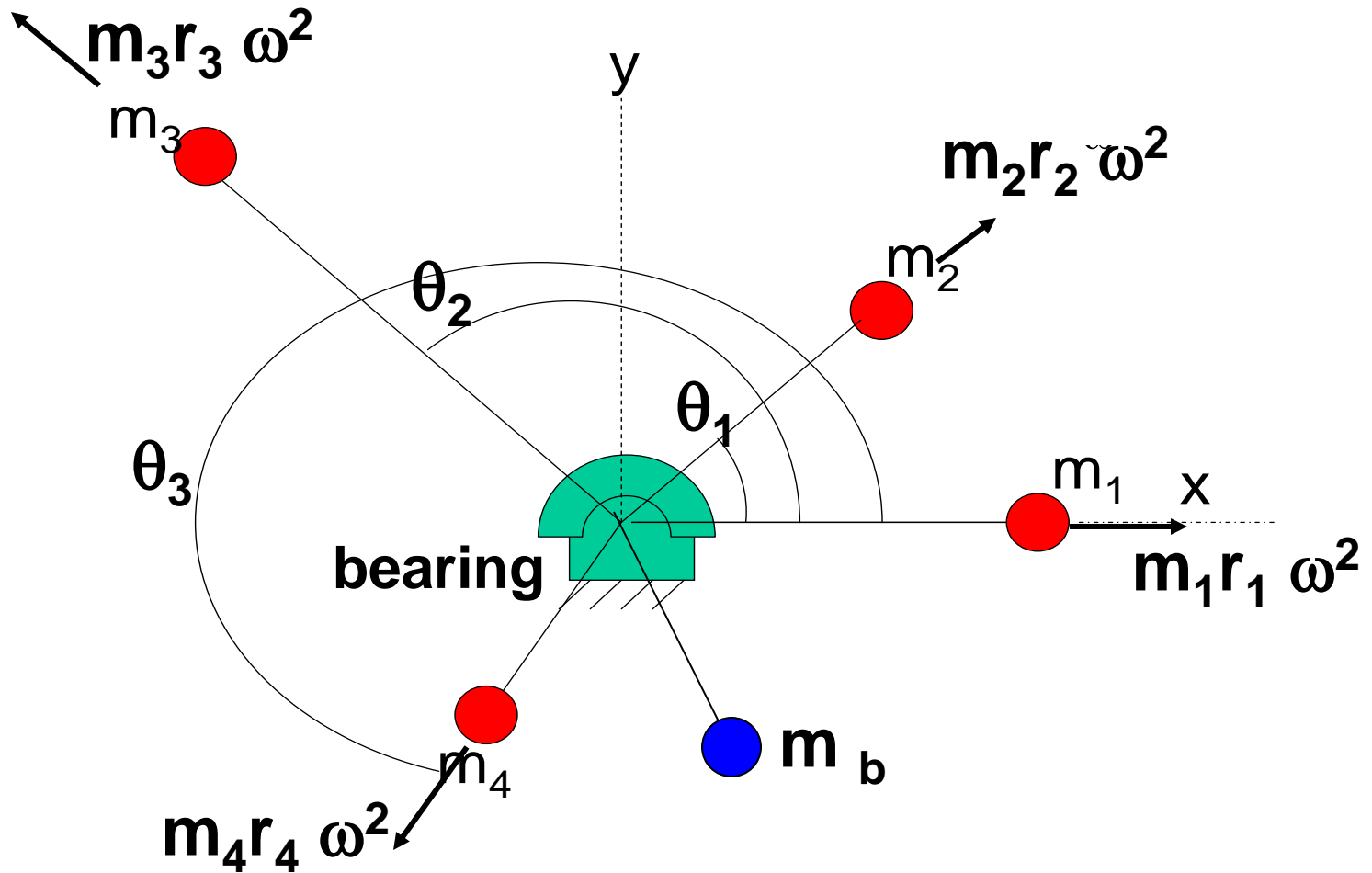
Magnitude of unbalance

Vibration occurs

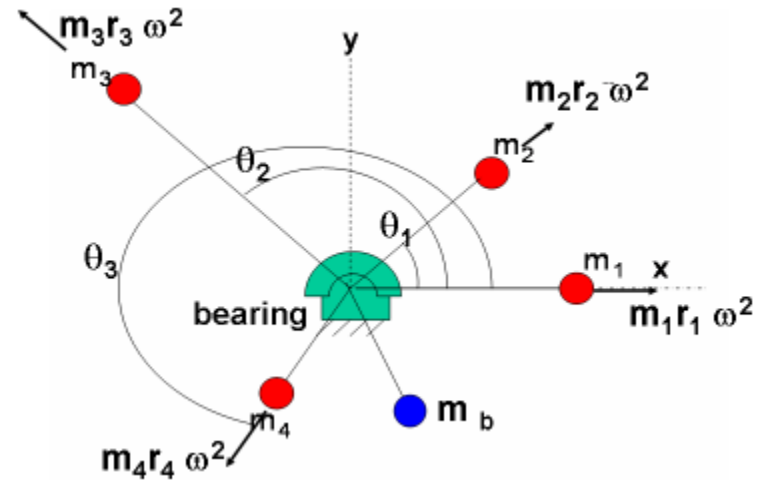
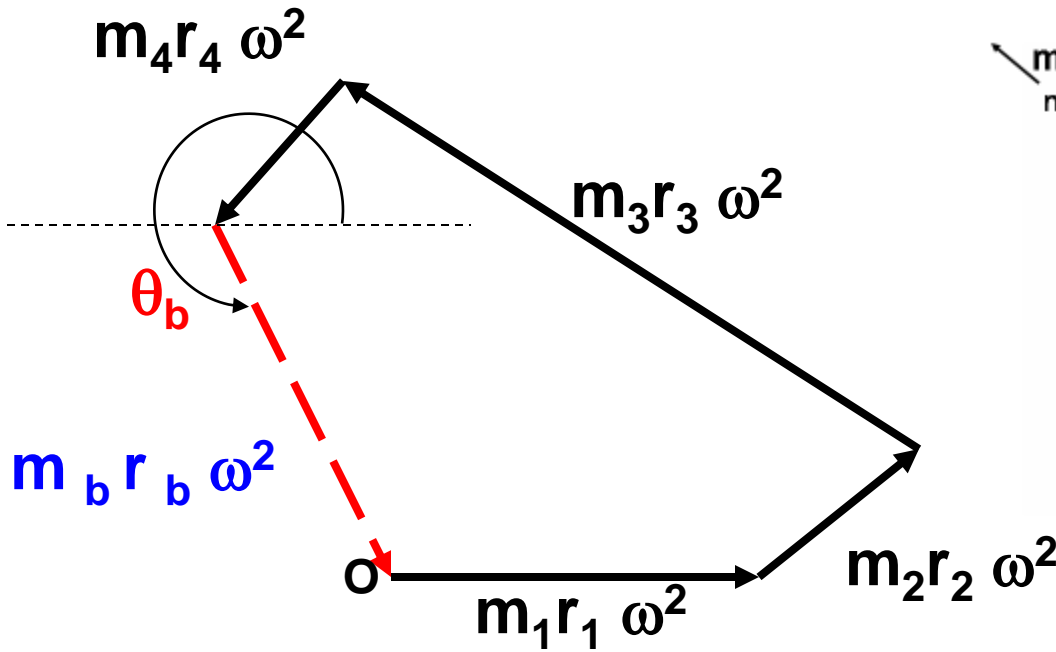
O_2

Elasticity of the bearing

Balancing of several masses revolving in the same plane using a Single balancing mass



Graphical method of determination
magnitude and
Angular position of the balancing mass



Force vector polygon

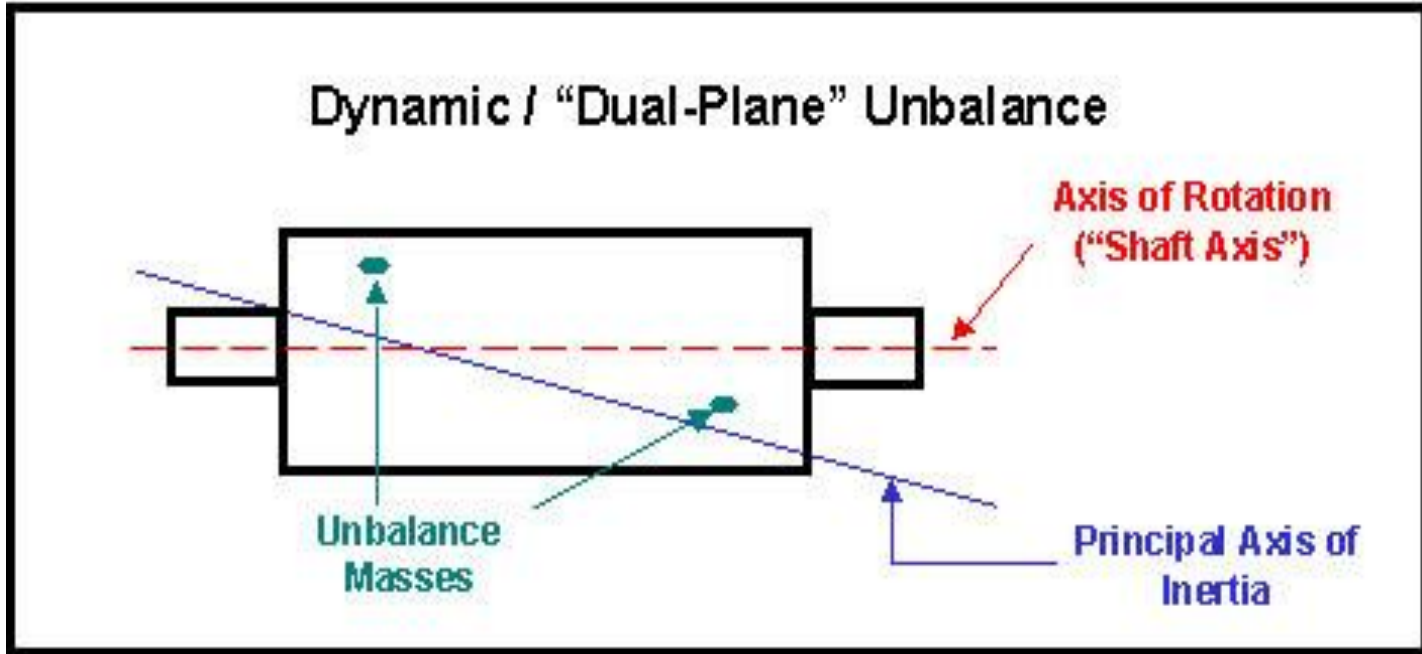
Determination of magnitude and Angular position of the balancing mass

$$\begin{aligned} m_1 r_1 \omega^2 \cos \theta_1 + m_2 r_2 \omega^2 \cos \theta_2 \\ + m_3 r_3 \omega^2 \cos \theta_3 + m_4 r_4 \omega^2 \cos \theta_4 \\ = m_b \cos \theta_b \end{aligned}$$

$$\begin{aligned} m_1 r_1 \omega^2 \sin \theta_1 + m_2 r_2 \omega^2 \sin \theta_2 \\ + m_3 r_3 \omega^2 \sin \theta_3 + m_4 r_4 \omega^2 \sin \theta_4 \\ = m_b \sin \theta_b \end{aligned}$$

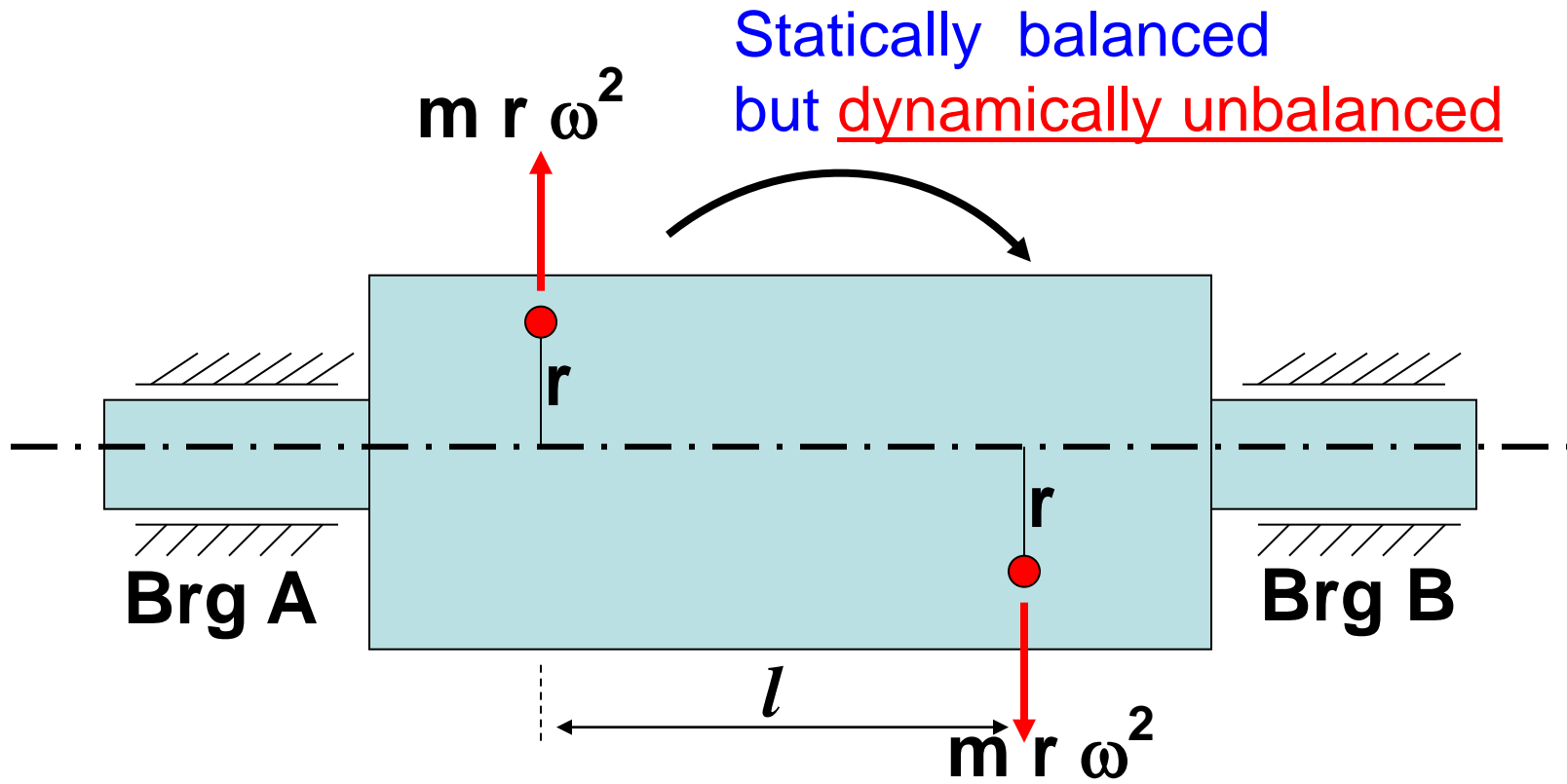
magnitude ' m_b ' and position ' θ_b ' can be determined by solving the above two equations.

Dynamic or "Dual-Plane" balancing



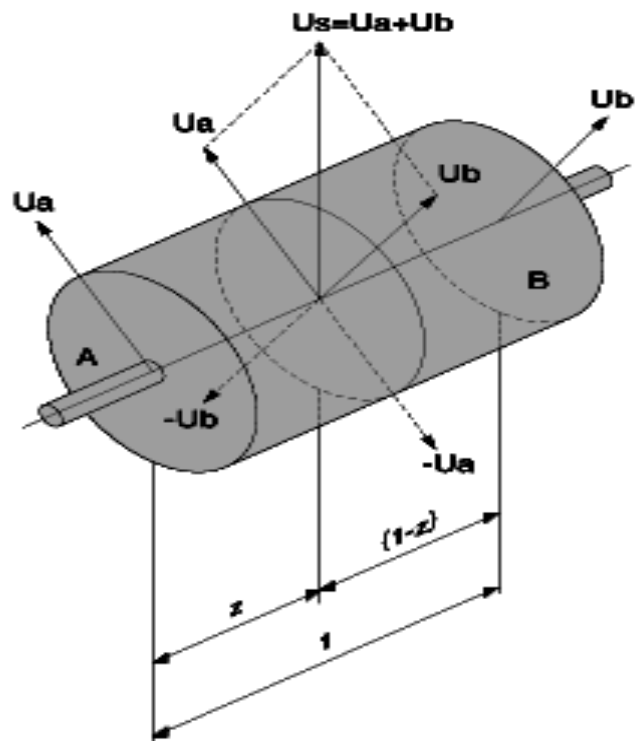
Dynamic balancing is required for components such as **shafts** and **multi-rotor assemblies**.

Dynamic or "Dual-Plane" balancing



Load on each support Brg

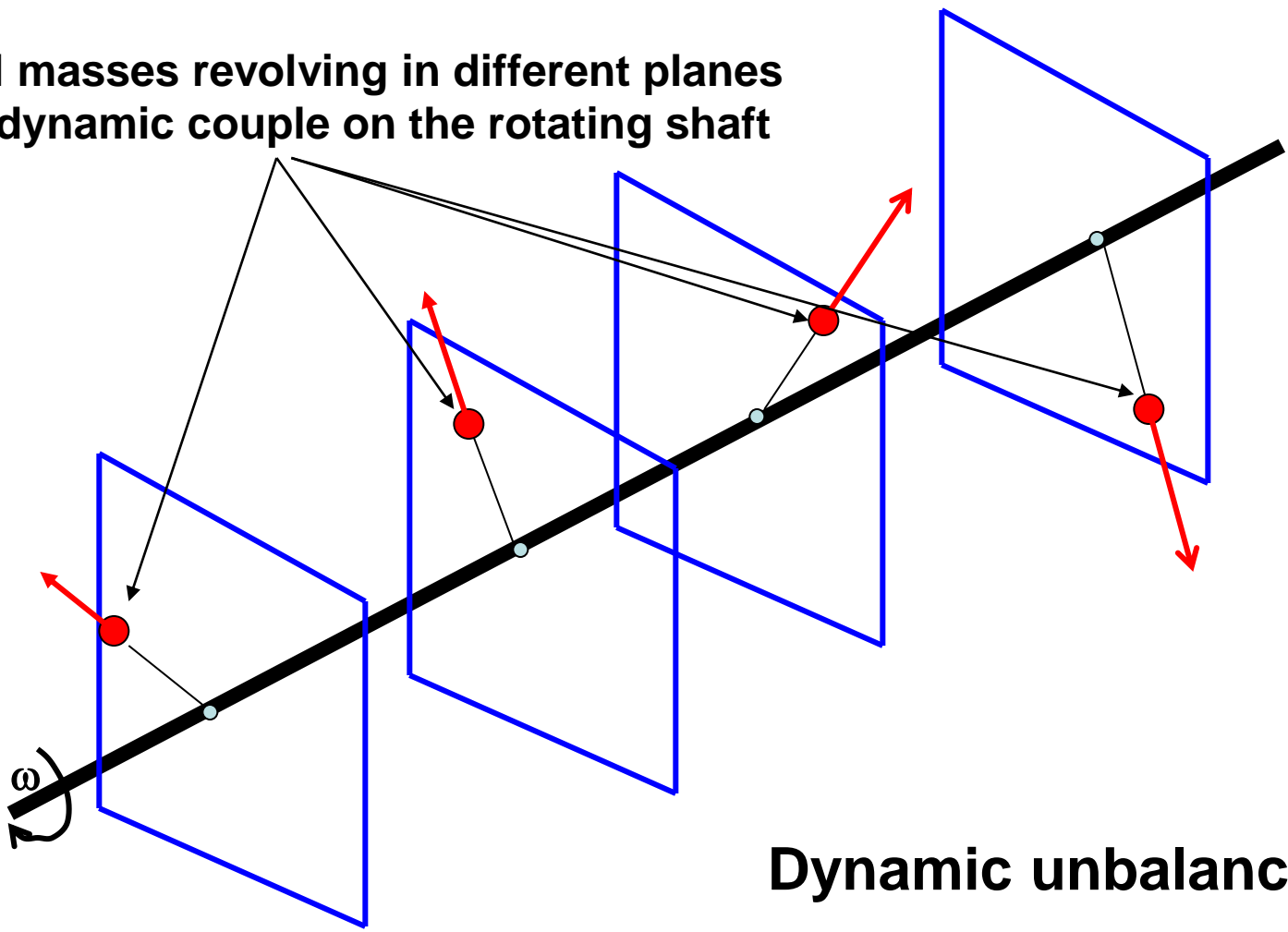
due to **unbalance** $= (m r \omega^2 l) / L$



Dynamic unbalances U_a and U_b on planes A and B respectively can be resolved to one static unbalance U_s which is equal to $U_a + U_b$ and a couple unbalance M which is equal to $U_b(1-z) - U_a z$

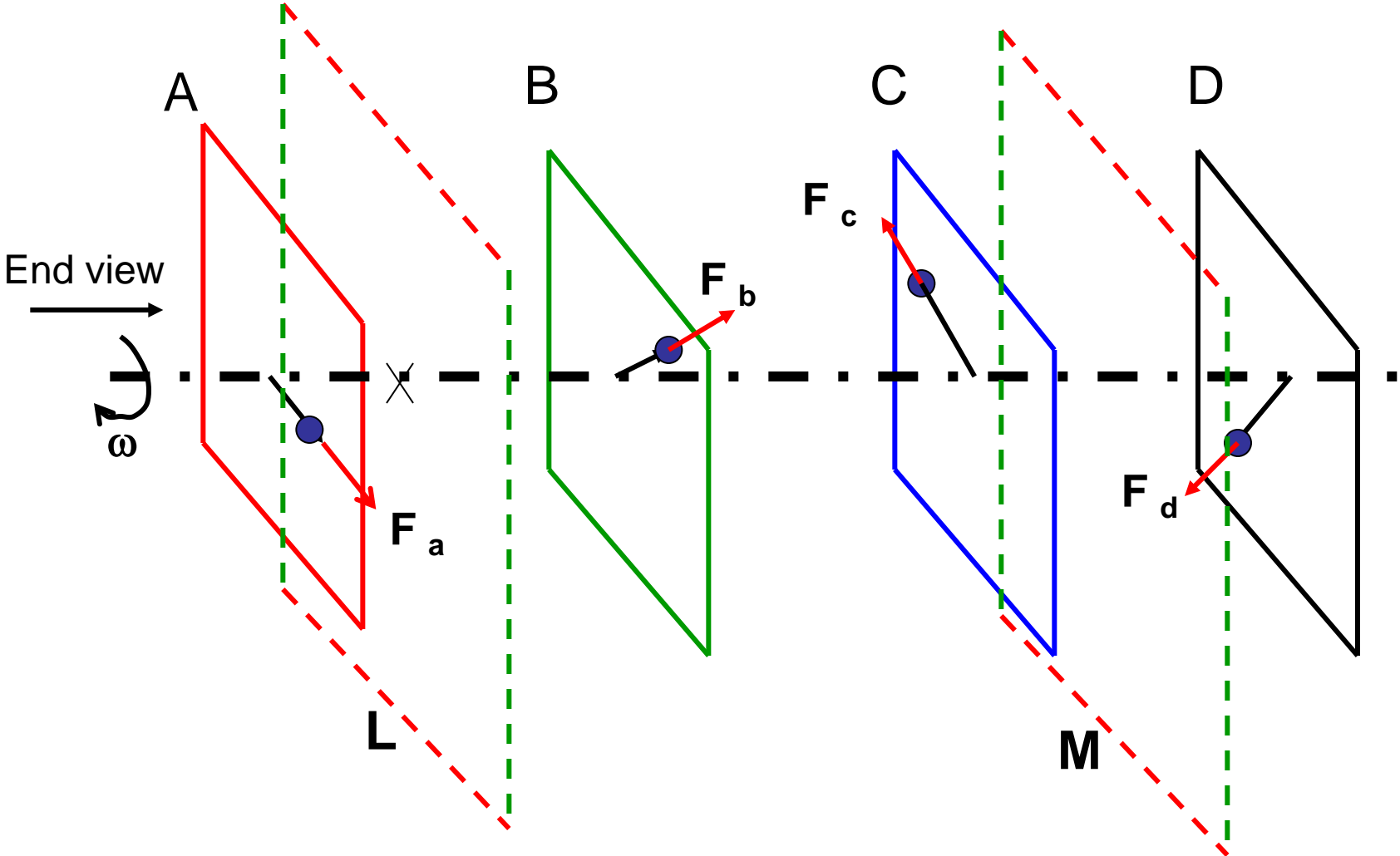
On an arbitrary plane C

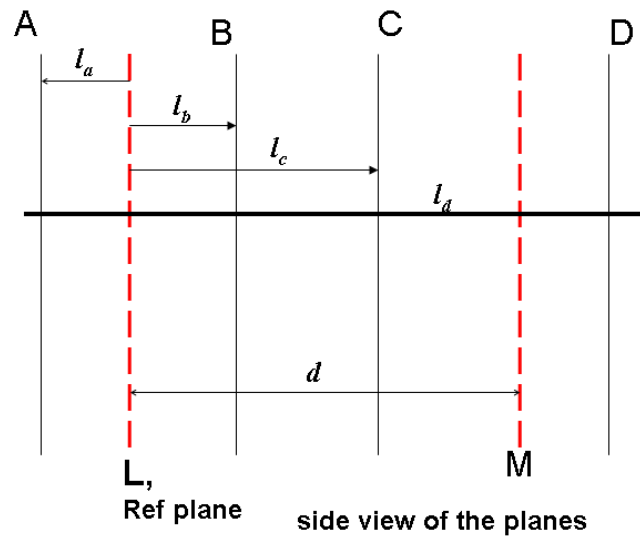
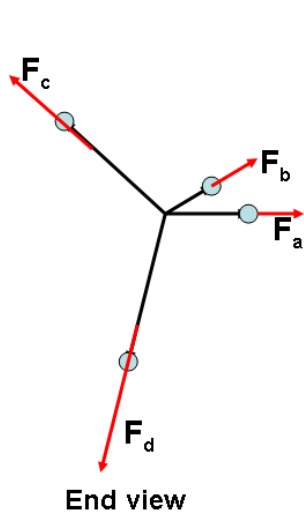
Several masses revolving in different planes
Apply dynamic couple on the rotating shaft



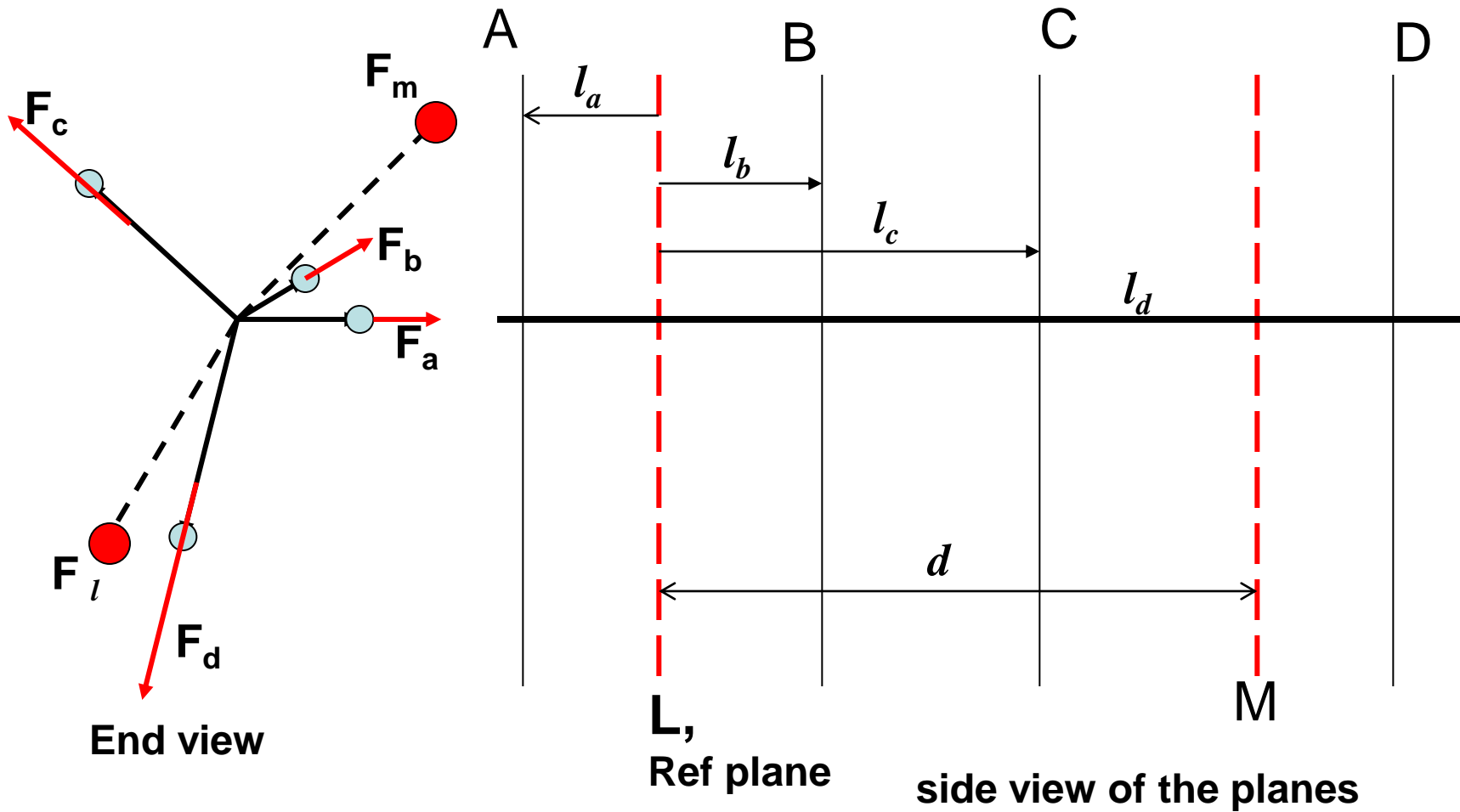
Dynamic unbalance

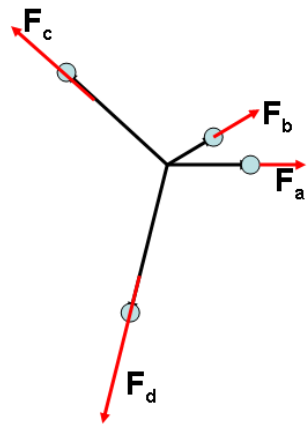
Balancing of several masses rotating in different planes



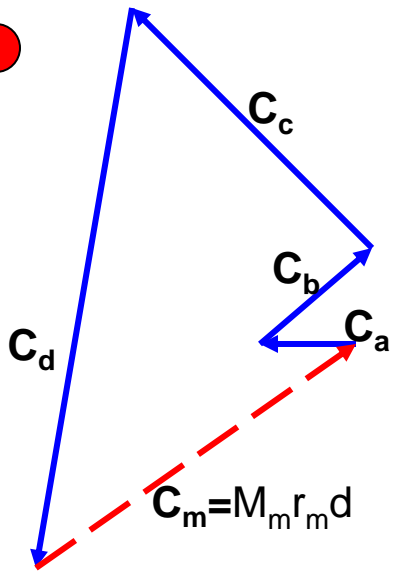
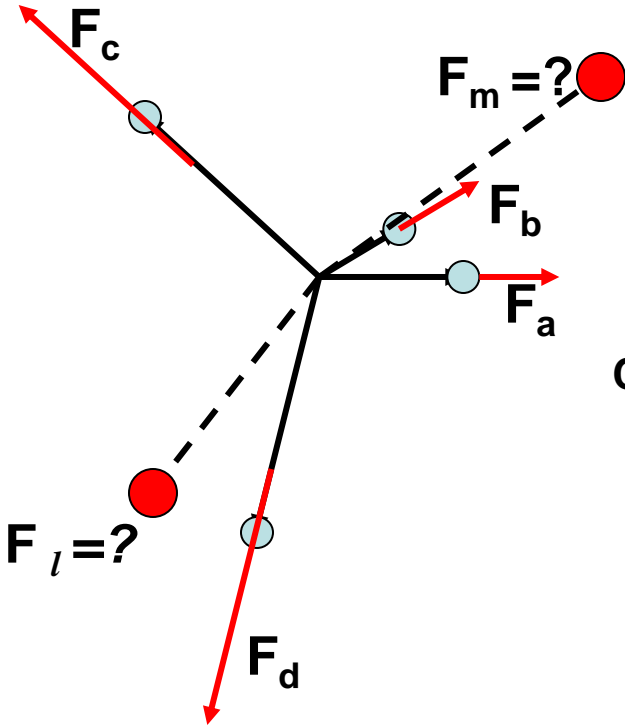
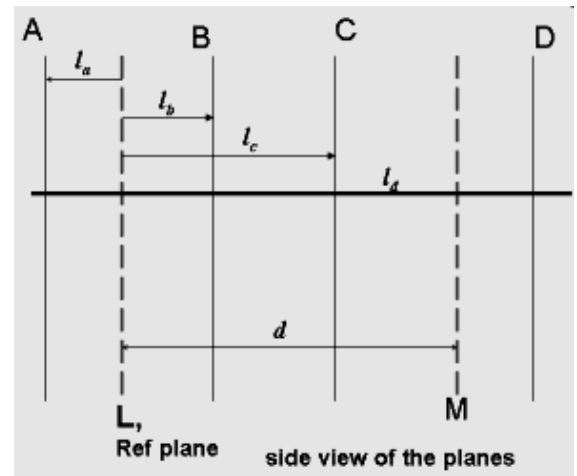


Plane	Mass M (kg)	Radius r (cm)	Force / ω^2 , $M r = F$, (kg. cm)	Dist. From ref plane l , (cm)	Couple / ω^2 $M r l = C$ (kg cm ²)
A	M_a	r_a	$M_a r_a$	$-l_a$	$-M_a r_a l_a$
L (Ref. plane)	M_l	r_l	$M_l r_l$	0	0
B	M_b	r_b	$M_b r_b$	l_b	$M_b r_b l_b$
C	M_c	r_c	$M_c r_c$	l_c	$M_c r_c l_c$
M	M_m	r_m	$M_m r_m$	d	$M_m r_m d$
D	M_d	r_d	$M_d r_d$	l_d	$M_d r_d l_d$

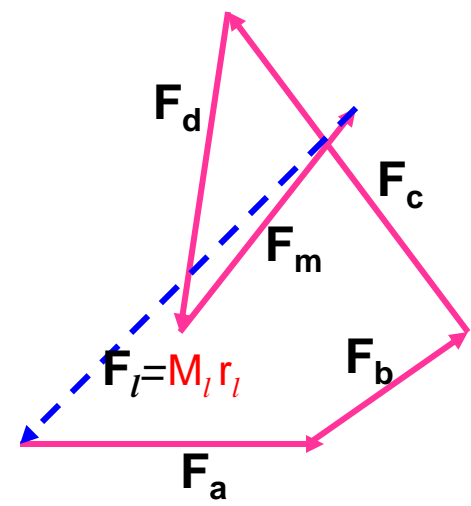




End view



Couple polygon



force polygon

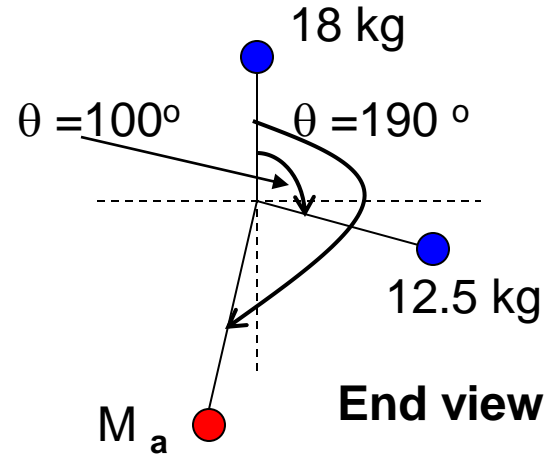
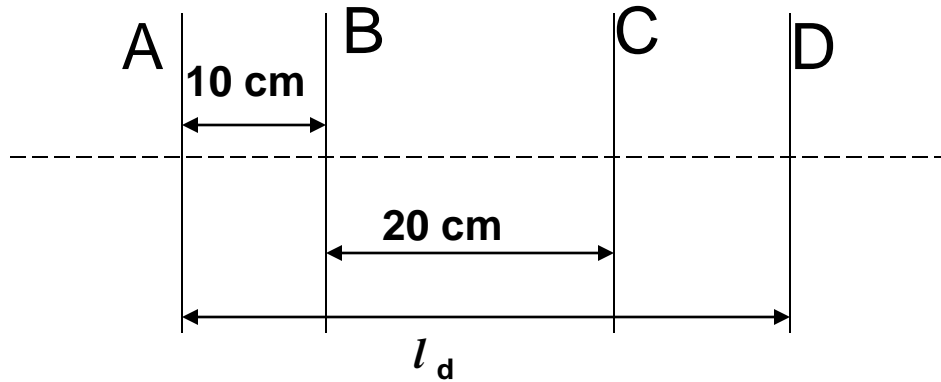
From couple polygon, by measurement, $C_m = M_m \times r_m \times d$
 From force polygon, by measurement, $F_l = M_l \times r_l$

Example :

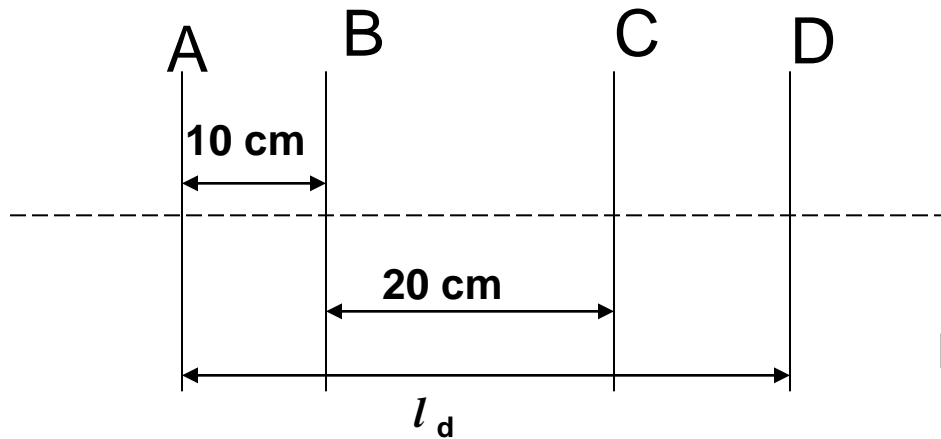
A shaft carries **four masses** in parallel planes **A,B,C,&D** in this order. The masses at B & C are 18 kg & 12.5 kg respectively and each has an eccentricity of 6 cm. The masses at A & D have an eccentricity of 8 cm. The angle between the masses at B & C is 100° and that between B & A is 190° both angles measured in the same sense. The axial dist. between planes A & B is 10cm and that between B & C is 20 cm. If the shaft is complete dynamic balance,

Determine,

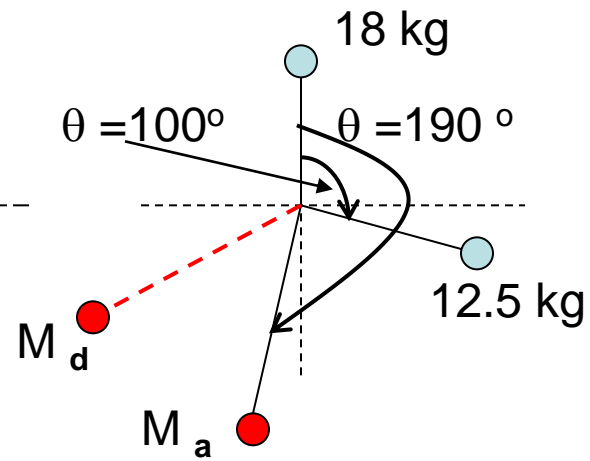
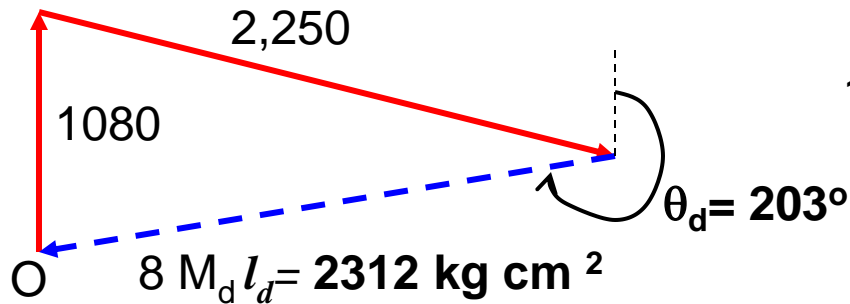
- 1 masses at A & D
2. Distance between plane C &D
3. The angular position of the mass at D



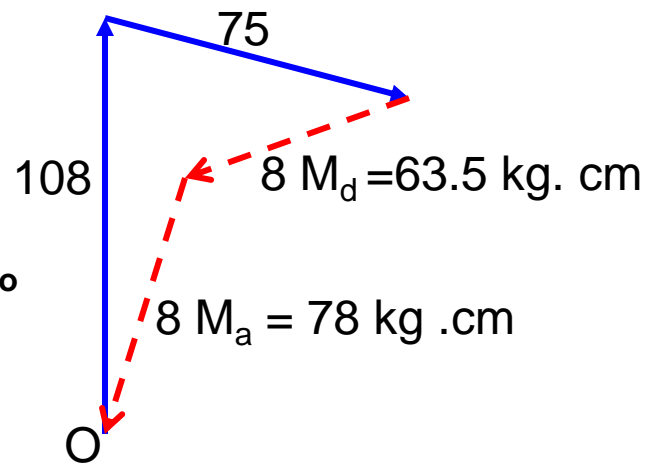
Plane	Mass M kg	Radius r cm	Force / ω^2 , $M r$, kg. cm	Dist. From ref plane 1, cm	Couple / ω^2 $M r l$ kg cm ²
A	$M_a=?$	8	$8 M_a$	0	0
B	18	6	108	10	1080
C	12.5	6	75	30	2250
D	$M_d=?$	8	$8 M_d$	$l_d=?$	$8 M_d l_d$



Couple polygon



force polygon



From the couple polygon,

$$\text{By measurement, } 8 M_d l_d = 2,312 \text{ kg cm}^2$$

$$\therefore M_d l_d = 2312 / 8 = 289 \text{ kg cm}$$
$$\theta_d = 203^\circ$$

From force polygon,

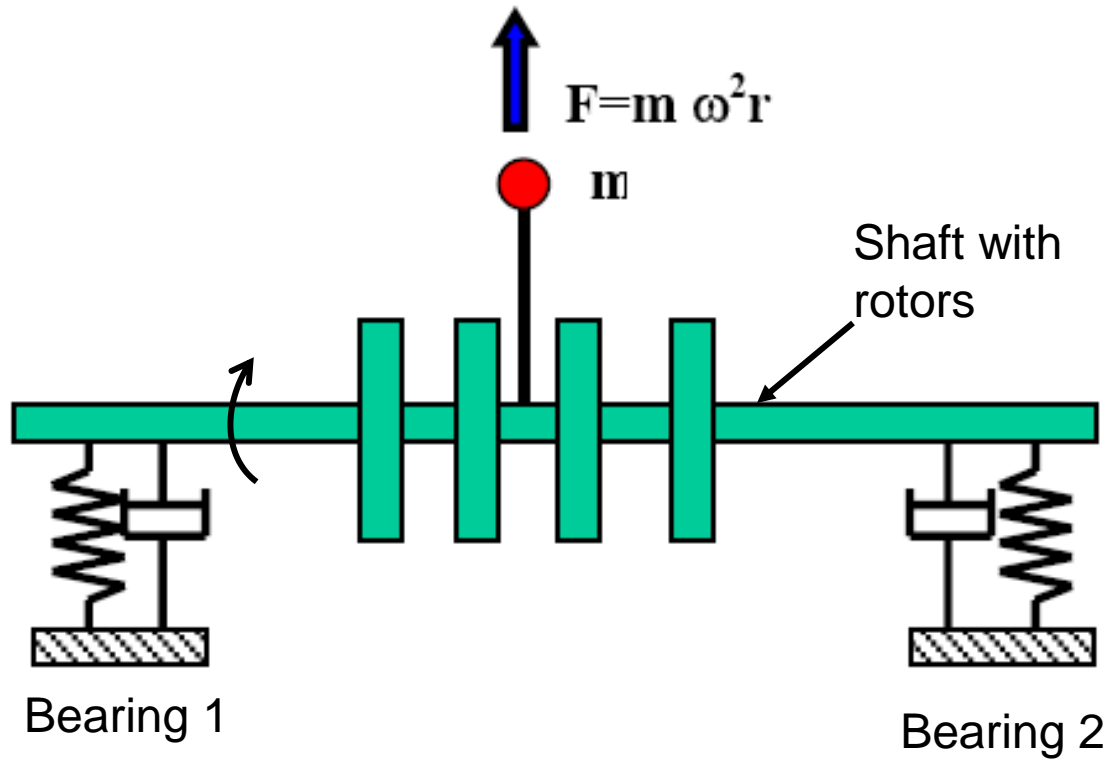
$$\text{By measurement, } 8 M_d = 63.5 \text{ kg cm}$$

$$8 M_a = 78.0 \text{ kg cm}$$

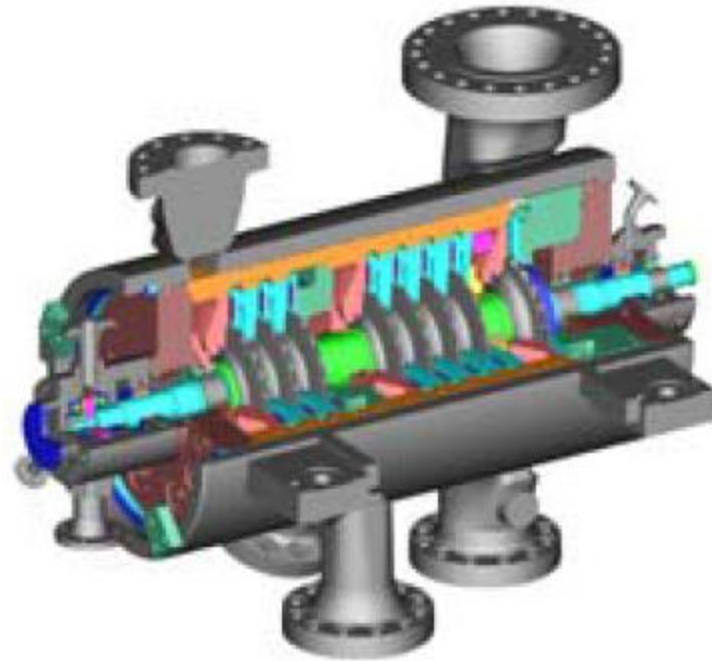
$$\underline{M_d = 7.94 \text{ kg}}$$

$$\underline{M_a = 9.75 \text{ kg}}$$

$$\underline{l_d = 289 / 7.94 = 36.4 \text{ cm}}$$



Unbalanced force on the bearing –rotor system



Cut away section of centrifugal compressor



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